

# Physics

Lesson Plan #2  
 A Mathematical Toolkit  
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## The Measures of Science

*Objectives: Define SI, metric prefixes, estimate measurements, scientific notation*

- Math – the language of Physics
- How would you measure without a ruler?
- 1795 the French adopted the Metric System which has become the Systeme Internaionale d’Unites – SI
- Standards are kept at the International Bureau of Weights and Measures in Sevres, France and in the National Institute of Science and Technology (NIST) in Gaithersburg Maryland
- Base Quantities are length, time, mass
  - o Length – meter
    - 1/10,000,000 distance from the north pole to the equator
    - Distance between two lines on a platinum-iridium bar
    - Distance light travels in a vacuum in 1/299,792,458 s
  - o Time – second
    - 1/86,400 of a mean solar day
    - frequency of cesium-133 atom
  - o Mass – kilogram
    - Platinum-iridium alloy cylinder
- Derived units are combinations of the base units.
  - o m/sec for speed,  $\text{kg}\cdot\text{m}^2/\text{s}^2$
- Which is more accurate – metric or English system?
  - o Accuracy is the same, metric is based on 10 making it easier to use
- SI Prefixes

Prefix	Symbol	Multiplier	Scientific Notation	Example
femto	f	1/1,000,000,000,000,000	$10^{-15}$	femtosecond (fs)
pico	p	1/1,000,000,000,000	$10^{-12}$	picometer (pm)
nano	n	1/1,000,000,000	$10^{-9}$	nanometer (nm)
micro	$\mu$	1/1,000,000	$10^{-6}$	microfarad ( $\mu\text{F}$ )
milli	m	1/1,000	$10^{-3}$	millimeter (mm)
centi	c	1/100	$10^{-2}$	centimeter (cm)
deci	D	1/10	$10^{-1}$	Deciliter (dL)
kilo	K	1000	$10^3$	Kilometer (km)
mega	M	1,000,000	$10^6$	Megabyte (Mb)
giga	G	1,000,000,000	$10^9$	Gigawatt (Gw)
tera	T	1,000,000,000,000	$10^{12}$	Terabyte (Tb)

-Examples

- 10 mm = 1 cm
  - 10 cm = 1 dm
  - 10 dm = 1 m
  - 1000 m = 1 km
- Scientific Notation
- Convenient way to express very large or very small numbers
  - $M \times 10^n$  where  $1 \leq M < 10$  and is multiplied by a whole number power of 10
  - Moving the decimal left, add to n. 1000. =  $1000 \times 10^0 \rightarrow 100 \times 10^1 \rightarrow 10 \times 10^2 \rightarrow 1 \times 10^3$
  - Moving the decimal right, subtract from n. .0001  $\rightarrow .0001 \times 10^0 \rightarrow .001 \times 10^{-1} \rightarrow .01 \times 10^{-2} \rightarrow .1 \times 10^{-3} \rightarrow 1 \times 10^{-4}$
  - Avg. distance from the sun to Mars is 227,800,000,000 m  $\rightarrow 2.278 \times 10^{11}$  m
  - The mass of an electron is 0.000,000,000,000,000,000,000,000,000,911 kg  $\rightarrow 9.11 \times 10^{-31}$  kg
  - Some calculators show scientific notation as  $ME^n$ , students should always write answer in full scientific notation ( $M \times 10^n$ )
- Addition and Subtraction Using Scientific Notation
- If numbers have the same exponent  $n$ , then add or subtract the values of  $M$  leaving  $n$  the same.
  - $4 \times 10^8 \text{ m} + 3 \times 10^8 \text{ m} = 7 \times 10^8 \text{ m}$
  - $4.1 \times 10^{-6} \text{ kg} - 3.0 \times 10^{-6} \text{ kg} = 1.1 \times 10^{-6} \text{ kg}$
  - $4.01 \times 10^6 \text{ m} + 1.89 \times 10^2 \text{ m} = 4.01 \times 10^6 \text{ m} - .000189 \times 10^6 \text{ m} = 4.01 \times 10^6 \text{ m}$  – do example of 240,000 +27 on calculator and on board
- Multiplication and Division Using Scientific Notation
- Multiply the value and units of  $M$ , add exponents  $n$ .
  - Divide the values and units of  $M$ , subtract the exponent  $n$  of the divisor from the exponent  $n$  of the dividend
  - $(4 \times 10^3 \text{ kg}) (5 \times 10^{11} \text{ m})$   
 $4 \times 5 = 20$ ,  $\text{kg} \times \text{m} = \text{kg} \bullet \text{m}$ ,  $3 + 11 = 14$   
 $20 \times 10^{14} \text{ kg} \bullet \text{m} = 2 \times 10^{15} \text{ kg} \bullet \text{m}$
  - $(8 \times 10^6 \text{ m}^3) / (2 \times 10^{-3} \text{ m}^2)$   
 $8/2 = 4$ ,  $6 - (-3) = 9$ ,  $3 - 2 = 1$   
 $4 \times 10^9 \text{ m}$
- Converting Units – Factor-Label Method
- Convert 465g  $\rightarrow$  kg
  - Setup a conversion factor of 1. Knowing that 1 kg = 1000g then we can construct  $1 = 1 \text{ kg}/1000 \text{ g}$  or  $1 = 1000\text{g}/1 \text{ kg}$
  - Multiplying or dividing by 1 does not change a value
  - Set up the conversion such that units cancel out:

- $465g = 465g \left( \frac{1kg}{1000g} \right) = \frac{465g \times 1kg}{1000g} = \frac{465kg}{1000} = 0.465kg$
- If units do not work out, check your conversion factor

- Example Problems

- 1.1 cm to meters
- $1.1cm = 1.1cm \left( \frac{1m}{100cm} \right) = \frac{1.1cm \times 1m}{100cm} = \frac{1.1m}{100} = \frac{1.1m}{10^2} = 1.1 \times 10^{-2} m$
- or  $1.1cm = 1.1cm \left( \frac{1m}{10^2 cm} \right) = \frac{1.1cm \times 1m}{10^2 cm} = \frac{1.1m}{10^2} = 1.1 \times 10^{-2} m$
- or  $1.1cm = 1.1cm \left( \frac{10^2 m}{1cm} \right) = \frac{1.1cm \times 10^2 m}{1cm} = \frac{1.1 \times 10^2 m}{1} = 1.1 \times 10^{-2} m$

- 76.2 pm to mm

- $76.2 pm = 76.2 pm \left( \frac{1m}{10^{12} pm} \right) \left( \frac{10^3 mm}{1m} \right) = \frac{76.2 pm \times 1m \times 10^3 mm}{10^{12} pm \times 1m} =$   
 $\frac{76.2 \times 10^3 mm}{10^{12}} = 76.2 \times 10^{-9} mm = 7.62 \times 10^{-8} mm$
- $76.2 pm = 76.2 pm \left( \frac{1mm}{10^9 pm} \right) = \frac{76.2 \times 1mm}{10^9} = \frac{76.2 mm}{10^9} =$   
 $76.2 \times 10^{-9} mm = 7.62 \times 10^{-8} mm$

- Precision and Accuracy

- Precision – the exactness of measurement (tolerance)
- Precision can be  $\frac{1}{2}$  the smallest division on the scale
  - Using round off to determine  $\frac{1}{2}$
  - On a typical meter stick, 1mm is the smallest division, therefore .5 mm is best precision
  - On a micrometer the smallest division is .01 mm, therefore .005 mm is the best precision
- Accuracy – how well the results agree with a standard value
  - Instrument must be calibrated to known standard

- Error

- Error = accepted value – experimental value
  - Can be positive or negative

- Percent Error

- Percent error =  $(\text{error} / \text{accepted value}) \times 100\%$

- Significant Digits – non-zero numbers

- Draw diagram of mm ruler, 8.64 cm bar and a cm ruler

- Note that the bar is 8.6 mm + a little by the mm ruler
- The little is estimated to be .4 mm
- So the length of the bar is 8.64 mm by the mm ruler – 8.6 can be seen, the .04 is an estimate
- Note that the bar is 8 + a little by the cm ruler
- The little is estimated to be .6 cm
- So the length of the bar is 8.6 cm by the cm ruler – 8. can be seen, the .6 is an estimate
- 8.64 is 3 significant figures, 8.6 is 2 significant figures
- Redraw to have the bar 8.60 in length – 8.60 is 3 significant figures
- Significant Digits – zero's
  - Not all 0's are significant
  - Place holders are not significant
    - 0.0086 = 2 significant figures
    - 0.00860 = 3 significant figures
    - 186,000 = 3, maybe six – unknown since the decimal is not shown
    - 186 km is 3sf, 186.000 is 6sf
    - $1.86 \times 10^5$  has 3 sf
- Rules for Significant Digits
  - Non-zero digits are always significant
  - All final 0's after the decimal point are significant
    - These are 0's after the final non-zero digit
  - Zero between two other significant digits are always significant
  - Zeros used solely as place holders are not significant
- The following examples have 3 significant digits
  - 245 m 18.0 g 308 km 0.00623 g
- Arithmetic with Significant Digits
  - An answer can never be more precise than the least precise number
- Addition & Subtraction
  - Add  $24.615 + 3.21 + 6.964 = 34.789$ 
    - Since 3.21 has the least number of digits to the right of the decimal, the correct answer is 34.79
    - Same principle for subtraction
- Multiplication & Division
  - $3.22 \text{ cm} \times 2.1 \text{ cm} = 6.762 \text{ cm}^2 \rightarrow 6.8 \text{ cm}^2$
  - Answer is rounded off to have the same number of significant digits as the factor with the least number of significant digits
  - $36.5 \text{ m} / 3.414\text{s} = 10.691 \text{ m/s} \rightarrow 10.7 \text{ m/s}$